## CS3231 : Tutorial - 8

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Q1: Show that EQ<sub>CFG</sub> is undecidable. Show that EQ<sub>CFG</sub> is co-Turing-recognizable.

**Q2** : Show that no computable function reduces  $A_{\mathsf{TM}}$  to  $E_{\mathsf{TM}}$ .

**Q3**: Show that if A is Turing-recognizable and  $A \leq_m \overline{A}$ , then A is decidable.

**Q4**: Show that the Post Correspondence Problem is decidable over the unary alphabet  $\Sigma = \{1\}$ . In the Silly Post Correspondence Problem, SPCP, in each pair the top string has the same length as the bottom string. Show that the SPCP is decidable.

**Q5** : Prove that there exists an undecidable subset of  $\{1\}^*$ .

**Q6** : Show that A is decidable iff  $A \leq_m 0^* 1^*$ .

**Q7**: Let  $S = \{\langle G \rangle : G \text{ is a CFG and } L(G) \text{ is unambiguous} \}$ . Show that S is not decidable.

**Q8**: Consider the problem of determining whether a PDA accepts some string of the form  $\{ww : w \in \{0,1\}^*\}$ . Use the computation history method to show that this problem is undecidable.