A P N E T 2 0 2 1

CONJECTURE: EXISTENCE OF NASH EQUILIBRIA IN MODERN INTERNET CONGESTION CONTROL

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THE INTERNET



TCP Reno

On Inferring TCP Behavior

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ABSTRACT

ABSTRACT Most of the triffs in dudy's itstenset is controlled by the Transmis-sion Control Protocol (TCP). Hence, the performance of TCP has significant impact on the performance of the overall Internet. TCP is a complex protocol with many uses configurable pranneners and times to produce on the development. In congestion, control mech-anisms and TCP options, and it is useful to trace the deployment of been env mere developments in congestion, control mech-anisms and TCP options, and it is useful to trace the deployment of these new mere developments in a congestion is control mech-anisms and TCP options, and it is useful to trace the deployment of the constraints in the Internet feels on the volumity is important to text. TCP implementations for conformant end-ored congestion control. Since web traffic forms the majority of the TCP traffic. TCP implementations in a body's web servers are of particular interact. TCPT implementations during a labor the TCP TCP interpre-tension is about the TCP behaviors of major web servers, obtained u-results about the TCP behaviors of major web servers, obtained u-ing that tool. We advective the user of TTHT is detect bags and

the overall congestion control behavior of the Internet is heavily influenced/by the TCP implementations in web servers, since a sig-milicant fraction of the traffic in the interest consists of TCP traffic methods and the traffic in the interest consists of TCP and the traffic in the traffic in the interest consists of TCP and the traffic in the traffic in the traffic in the traffic interest parameters. A host of variations on the basic conges-pticate of the traffic in the traffic in the traffic interest picture of TCP performance, analysis and immlations must be ac-picate to a Selective Acknowledgement (5ACK) and Ex-plicit Congestion Notification (ECN). To obtain a comprehensive or to develop TBIT. To answer questions such as "h ap-propriate to base Internet simulation and analyzers in the article and or TCP enginesis controf from [900 hap performs particularly badly when multiple packets are despend from a window of data.

[2001] Padhya et al.

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TCP CUBIC

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TCP Congestion Avoidance Algorithm Identification Peng Yang. Member, IEEE, Juan Shao, Wen Luo, Lisong Xu, Member, IEEE, Jinender Deogun, Member, IEEE, and Ying Lu, Member, IEEE

Abstract—The Interact has recently been evolving from homog- neous compation control to heterogeneous congestion control. Ser- eral years aga, interact traffet was madely controlled by the tradi- tic programme and the series of the series of the series of the TCP algorithms, such as RENO, CUBC, and Compound TCP (TCP). However, here is very lith works on the performance and stability oftal of the interact with heterogeneous congestion con- mation of different TCP algorithms. In this paper, we first pro- mation of different TCP algorithms.	TCP ALCONTING AVAILATE IN MACH OPERATING SYSTEM FAMILIES Operating System TCP Japoint Windows Imily RESO [2], and TCP [3] Handrow Imily RESO [2], and TCP [3] Lam Cole (1), HTCP 114, HTCP 1					
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Index Terms—Heterogeneous congestion control, Internet mea- surement, TCP congestion control.	person living at a house, the process of obtaining the tCP de- ployment information can be considered as the TCP algorithm census in the country of the Internet. Just like the population consus is vital for the study and planning of the society. the					
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T HE INTERNET has recently been evolving from homo- geneous congestion control to heterogeneous congestion control A few years are intermet traffic was mainly controlled	Question 1: Ar trolled by Reno?: of recently propos	e the Majority of TCP Flows Still Con- This is an important question because most ed congestion control algorithms, such as				

The IR NTERNET has recently been covering from homocontrol. A few years ago, Internet traffic was mainly controlled by Rono¹¹. This is an impettant question because most control. A few years ago, Internet traffic was mainly controlled or forcently proposed conjection control algorithms, such as by the same TCP conjection control algorithm—the standard COBIG (7), TCP [8], DCCP [9], and CSEP Additive-Increase-Multiplicative-Decrease algorithm [2], [3] to perform well when competing with the trafficional RENO. If which is usually called RENO 11 Housever Internet Infile is but velo friendly with the competing RENO traffic (usually response). [2011] Yang et al.

ТНЕ INTERNET



MEASURING

BOTTLENECK BANDWIDTH

PROPAGATION

petabytes of data with global collaborators but find their carefully engineered multi-Gbps infrastructure

TIME



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	eral years ago, Internet traffic was mainly controlled by the tradi-	Operating Systems	TCP algorithms
	tional RENO, whereas it is now controlled by multiple different	Windows family	RENO [2], and CTCP [8]
	TCP algorithms, such as RENO, CUBIC, and Compound TCP	Linux family	RENO, BIC [12], CUBIC [13], HSTCP [14],
	(CTCP). However, there is very little work on the performance and		HTCP [15], HYBLA [16], ILLINOIS [17],
	stability study of the internet with neterogeneous congestion con-		LP [18], STCP [19], VEGAS [20], VENO [21],
	mation of different TCP algorithms. In this paper, we first pro-		WESTWOOD+ [22], and YEAH [23]
	pose a tool called TCP Congestion Avoidance Algorithm Identifi-		
	cation (CAAI) for actively identifying the TCP algorithm of a re-		
	mote Web server. CAAI can identify all default TCP algorithms	users can change t	heir TCP algorithms with only a single lin
10000	(e.g., RENO, CUBIC, and CTCP) and most non-default TCP al-	of command, Linu	x developers can even design and then ad-
ABSTR	gorithms of major operating system families. We then present the	their own TCP ale	orithms
Most of the	CAAI measurement result of about 50 000 web servers, we found that only 3 31% as 14 47% of the Wab servers still use RENO	There is, howeve	er, very little work [4]-[6] on the performance
sion Contri	46.92% of the Web servers use BIC or CUBIC, and 14.5% ~	and stability study	of the Internet with heterogeneous conges
significant	25.66% of the Web servers use CTCP. Our measurement results	tion control. One fi	undamental reason is the lack of the deploy
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tinues to p	control has changed from homogeneous to heterogeneous.	node as a house a	nd a TCP algorithm running at a node as
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24th June 2021, Ayush Mishra, NUS - APNet '21

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A SMALL NUMBER OF BBR FLOWS CAN BE VERY COMPETITIVE AGAINST CUBIC



Most early deployment results from Google, Dropbox and Spotify cite better throughput as a reason to switch to BBR.

How will these benefits sustain as more and more people catch on?



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Problem Statement:

HOW DO WE EXPECT THE INTERNET TO EVOLVE?

Would it be reasonable to expect the whole Internet to switch to BBR or its variants, in the near future?

We can model the Internet as a normal form game!



In game theory, a normal form game is a standard representation of a game where the players have some preference of outcome, which in this case is throughput



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Strategies:



TCP BBR

Known Interactions between CUBIC and BBR

Throughput in relation to buffer size

- Since CUBIC is loss based, it is able to outperform BBR in deep buffers by placing a lot of packets in the bottleneck buffer.
- On the other hand, in shallow buffers, CUBIC loses out to BBR because of frequent packet losses.

Observation 1. When competing at the bottleneck where the buffer is deep, CUBIC tends to have higher throughput than BBR; the converse is true when the buffer is shallow.

Throughput in relation to buffer size



Fig. 1. BBR throughput vs. bottleneck buffer size.

• Therefore, there must be some buffer size T_{fair} where the throughput of the two competing flows must be the same!

Observation 2. When a single BBR flow competes with a single CUBIC flow at a bottleneck, there must exist some threshold bottleneck buffer size T_{fair} such that when the bottleneck buffer size $Buff < T_{fair}$, the BBR flow gets higher throughput than the CUBIC flow and when $Buff > T_{fair}$, the CUBIC flow gets higher throughput than BBR.

Throughput in relation to number of flows $\[figs]$



Fig. 2. BBR's throughput vs. % of BBR flows.

Empirically, we can also observe that as the percentage of BBR flows at the bottleneck increases, their per-flow average throughput reduces.

Observation 3. As the percentage of BBR flows at the bottleneck increases, the per-flow average throughput of BBR flows at that bottleneck decreases.

Throughput in relation to RTT

- CUBIC flows with a smaller RTT are able to probe much faster than flows with longer RTTs due to frequent feedback.
- BBR flows with longer RTT are able to get higher bandwidth than flows with smaller RTTs because they place 1 BDP worth of packets in the bottleneck buffer

Observation 4. When two BBR flows compete at a bottleneck, the flow with a longer RTT will get higher bandwidth than the flow with a shorter RTT. When two CUBIC flows compete at a bottleneck, the flow with a shorter RTT will get higher bandwidth than the flow with a longer RTT.

Using these observation to predict a Nash Equilibrium in a 2 flow game

A Nash Equilibrium in a game is a strategy distribution between the players where no player has anything to gain by changing only their strategy.

	$Buff < T_2$			$T_2 < Buff < T_3$			$T_3 < Buff$					
Scenario	Strategies		Outcome		Strategies		Outcome		Strategies		Outcome	
1 2 3 4	$\begin{vmatrix} S_1 \\ C \\ C \\ B \\ B \end{vmatrix}$	S ₂ C B C B	S ₁ L L W W	S_2 W W L	<i>S</i> ₁ C C B	S ₂ B C B	S_1 L W W	S_2 W L L	<i>S</i> ₁ C B B	S ₂ C B C B	S ₁ L W L	S_2 W L W
Nash Equilibrium		2										

Table 2. Outcomes in a two-flow game. ($RTT_1 > RTT_2$, winning strategies are highlighted)

Nash Equilibria in a general *n*-flow game

- The complete mathematical proof is beyond the scope of this work, we therefore make the conjecture that a NE will exist in an n-flow game
- This conjecture is based on the observation that BBR flows get diminishing returns in throughput as the percentage of flows at the bottleneck increase



Fig. 3. Sub-linear increase in total BBR bandwidth.

Checking the claims of this conjecture in a limited state space

- We ran various number of flows through a common bottleneck link and measured their throughputs.
- For a given number of flows and a network configuration we ran all the possible combinations of flows running either CUBIC or BBR.
- A given distribution of CUBIC and BBR was considered to be the NE if in that combination, all of the flows got worse throughput if they switched their congestion control algorithm (while everyone else ran the same CC)

CBC

Is the NE if:

In BBC, flow 1 gets worse throughput In CCC, flow 2 gets worse throughput In CBB, flow 3 gets worse throughput

Properties of observed NE

- NE was computed in 6, 9 and 12 flow systems with each third of the flows having RTTs 20, 50 and 80 ms respectively
- In each case, we observed exactly one Nash Equilibrium
- In each Nash Equilibrium, when the flows were sorted by the RTT, CUBIC was always picked by the smallest RTT flows

(CCC...)(...BBB)

m flows

(n-m) flows

Effect of buffer size and link speed on the NE



Fig. 4. The effect of link capacity and number of flows on the Nash Equilibrium. RTTs 20 ms, 50 ms and 80 ms.

- Buffer size had the biggest effect on where the NE was
- At high buffer sizes, the NE seems to be at a 50-50 split between CUBIC and BBR

Effect of RTT distribution on the NE



Fig. 5. The effect of the RTT distribution on the Nash Equilibrium.

RTT distribution had a small effect of the where the NE was

Conclusion

- Despite BBR's current throughput benefits, CUBIC is unlikely to disappear soon from the Internet
- The Internet is likely to remain a heterogeneous mix of congestion control algorithms
- TCP performance is highly contextual

Future work

- Formal proof for NE is a general n-flow game
- The Internet does not follow economic game theory
- Effect on the NE in the presence of multi-hop paths, large number of flows and AQMs

Thank you! Questions?