## NATIONAL UNIVERSITY OF SINGAPORE

## CS1231 - Discrete Structures

(Semester 1: AY2018/19)

## ANSWER SHEETS

Time Allowed: 2 Hours

## INSTRUCTIONS TO CANDIDATES

1. These Answer Sheets consist of FIVE (5) printed pages.
2. Fill in your Student Number clearly below with a pen. Do NOT write your name.
3. You may write your answers in pencil.

## STUDENT NUMBER:


(Write your Student Number above legibly with a pen.)

| FOR EXAMINER'S USE ONLY |  |  |
| :---: | :---: | :---: |
| Questions | Max. | Marks |
| MCQs (Q1-15) | 30 |  |
| Q16 | 14 |  |
| Q17 | 14 |  |
| Q18 | 12 |  |
| Total | 70 |  |

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## Section B (40 marks)

Q16.
(a)
[2]

(b)
[2]

(c) How many slips have a 2 written on them?
[2]
(d) i .

| Probability of getting a head. |
| :--- |
|  |

ii. Probability that coin is two-headed.
(e).

|  | Pigeonhole Principle |
| :--- | :--- |

(a)

2] Express $E(n)$ in terms of $V_{3}(n)$ and $V_{4}(n)$.
[2]
]
(b) Recurrence relation for $V(n)$ for $n>0$.
[2]
(c) Closed form formula for $V(n)$ for $n \geq 0$.
[2]
(d) $\quad$ Recurrence relation for $E(n)$ for $n>0$.
[2]
[2]
(e) Closed form formula for $E(n)$ for $n \geq 0$.
2]
(f) $\quad$ Relate $v, e$ and $f$ in Euler's formula $v-e+f=2$ with the functions defined in this question.
(g)
[2] $\quad$ Closed form formula for $P(n)$ for $n \geq 0$.

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Q18.
(a) Checksum letter for SCS1231.
[2]
$\qquad$
(b) Show that $f$ is not one-to-one.
[2] $\qquad$
(c)
[8]

