## NATIONAL UNIVERSITY OF SINGAPORE

# **CS1231S – DISCRETE STRUCTURES**

(Semester 2: AY2021/22)

## **ANSWER SHEETS**

Time Allowed: 2 Hours

#### **INSTRUCTIONS**

- 1. These ANSWER SHEETS consist of **SIX (6)** printed pages.
- 2. Answer **ALL** questions on these Answer Sheets. You are to submit only these Answer Sheets and not the question paper. You may write in pen or pencil.
- 3. Printed/written materials are allowed. Apart from calculators, electronic devices are not allowed.
- 4. The maximum mark of this assessment is 100.
- 5. Do <u>not</u> write your name. Write your Student Number (eg: A0123456X) below.

| А | 0 |  |  |  |  |  |  |  |
|---|---|--|--|--|--|--|--|--|
|---|---|--|--|--|--|--|--|--|

#### === END OF INSTRUCTIONS ===

#### For internal use only

| MCQs | MRQs | Q17 | Q18  | Q19  | Q20  | Q21 | Total       |
|------|------|-----|------|------|------|-----|-------------|
| (20) | (18) | (5) | (10) | (20) | (20) | (7) | (100 marks) |
|      |      |     |      |      |      |     |             |

Write your answers for MCQs and MRQs in the boxes below, in **CAPITAL LETTERS**:



### PART C:

**Q17.** Prove by mathematical induction: 7 |  $(5^{2n+1} + 2^{2n+1})$  for all  $n \in \mathbb{N}$ .

[5 marks]

[Total: 10 marks]

# Q18.

| (a) [6] |       | ls injective?<br>(Write "true" or "false") | Is surjective?<br>(Write "true" or "false") |
|---------|-------|--------------------------------------------|---------------------------------------------|
|         | (i)   |                                            |                                             |
|         | (ii)  |                                            |                                             |
|         | (iii) |                                            |                                             |

# (b) [2]

| (c) [2] |         |      |  |
|---------|---------|------|--|
| (c) [2] |         |      |  |
| (c) [2] |         |      |  |
|         | (c) [2] | <br> |  |

Q18 Total: /10



| Q20.    |                                                           |
|---------|-----------------------------------------------------------|
| (a) [3] | Non-isomorphic, connected simple graphs on four vertices. |

[Total: 20 marks]

(b) (i) [2]. (...graph K<sub>2,4</sub>) (b) (ii) [2]. (...graph K<sub>3,4</sub>) (b) (iv) [2] (...graph  $K_5 - \{e\}$ ) (b) (iii) [2]. (...5 vertices, 8 faces)

# (c) [Subtotal: 9](i) [3] (Fill in the edges in the graph *G*)

| $\stackrel{T_1}{O}$         | <i>T</i> <sub>7</sub><br>O | T <sub>6</sub><br>O | T <sub>8</sub><br>O | T <sub>3</sub><br>O |
|-----------------------------|----------------------------|---------------------|---------------------|---------------------|
| ${\mathop{O}\limits_{T_4}}$ | O<br>T <sub>10</sub>       | $O T_5$             | O<br>T <sub>2</sub> | O<br><i>T</i> 9     |

(ii) [2]. (Colour the graph *G* above that you have obtained in part (i). If you do not have colour pens/pencils, you can label the vertices with colour labels C1, C2, C3, C4, etc.)

#### (iii) [2]

| (iv) [2] | (use a minimum | number | of machines) |  |
|----------|----------------|--------|--------------|--|

| Machine | Tasks Assigned |  |
|---------|----------------|--|
| M1:     |                |  |
| M2:     |                |  |
| :       |                |  |
| :       |                |  |
| :       |                |  |
| :       |                |  |
|         |                |  |

# Q21.

#### === END OF ANSWER SHEETS ===