## NATIONAL UNIVERSITY OF SINGAPORE

## CS1231S - DISCRETE STRUCTURES

(Semester 2: AY2021/22)

## ANSWER SHEETS

Time Allowed: 2 Hours

## INSTRUCTIONS

1. These ANSWER SHEETS consist of SIX (6) printed pages.
2. Answer ALL questions on these Answer Sheets. You are to submit only these Answer Sheets and not the question paper. You may write in pen or pencil.
3. Printed/written materials are allowed. Apart from calculators, electronic devices are not allowed.
4. The maximum mark of this assessment is 100.
5. Do not write your name. Write your Student Number (eg: A0123456X) below.

| $A$ | 0 |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

For internal use only

| MCQs <br> $(20)$ | MRQs <br> $(18)$ | Q17 <br> $(5)$ | Q18 <br> $(10)$ | Q19 <br> $(20)$ | Q20 <br> $(20)$ | Q21 <br> $(7)$ | Total <br> $(100$ marks $)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |

## CS1231S

Write your answers for MCQs and MRQs in the boxes below, in CAPITAL LETTERS:

## PART A:

1 $\square$
2 $\square$
3

4

5

6 $\qquad$
7 $\square$
8

9 $\square$
10


## PART B:

11 $\square$
12 $\square$
13 $\square$
14 $\square$
15 $\square$
16 $\square$

PART C:
Q17. Prove by mathematical induction: $7 \mid\left(5^{\mathbf{2 n + 1}}+\mathbf{2}^{2 n+1}\right)$ for all $n \in \mathbb{N}$.

Q18.
[Total: 10 marks]
(a) [6]

|  | Is injective? <br> (Write "true" or "false") | Is surjective? <br> (Write "true" or "false") |
| :---: | :---: | :---: |
| (i) |  |  |
| (ii) |  |  |
| (iii) |  |  |

(b) [2]

(c) [2]


Q19.

(ii) $\square$
(iii) $\square$
(b) (i)

(ii)
[3]

(c) (i)

(ii)

(iii)
[3]

(d) (i)

(ii) Write your explanation below.
[3]

(a) [3] Non-isomorphic, connected simple graphs on four vertices.
$\square$
(b) (i) [2]. (...graph $K_{2,4}$ )
(b) (ii) [2]. (...graph $K_{3,4}$ )
(b) (iii) [2]. (... 5 vertices, 8 faces)
(b) (iv) [2] (...graph $K_{5}-\{e\}$ )
(c) [Subtotal: 9]
(i) [3] (Fill in the edges in the graph $G$ )

| $T_{1}$ | $T_{7}$ | $T_{6}$ | $T_{8}$ | $T_{3}$ |
| :--- | :--- | :--- | :--- | :--- |
| $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
|  |  |  |  |  |
| $T_{4}$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
|  | $T_{10}$ | $T_{5}$ | $T_{2}$ | $T_{9}$ |
|  |  |  |  |  |

(ii) [2]. (Colour the graph $G$ above that you have obtained in part (i). If you do not have colour pens/pencils, you can label the vertices with colour labels C1, C2, C3, C4, etc.)
(iii) [2]
$\square$
(iv) [2] (use a minimum number of machines)

Machine Tasks Assigned
M1: $\qquad$
M2: $\qquad$
$\qquad$ : $\qquad$
$\qquad$ : $\qquad$
$\qquad$ : $\qquad$
$\qquad$
: $\qquad$

