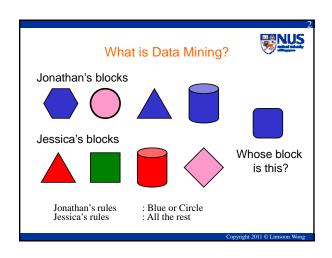
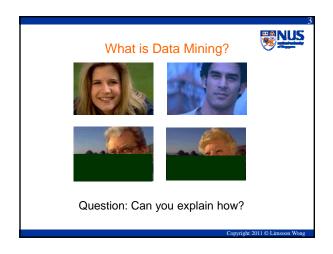
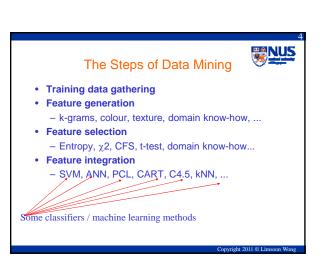
For written notes on this lecture, please read chapter 3 of The Practical Bioinformatician,

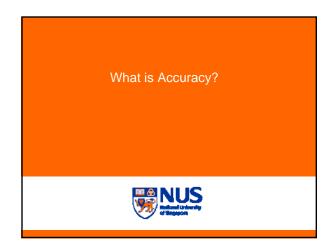
CS2220: Introduction to Computational Biology
Lecture 1: Essence of Knowledge Discovery

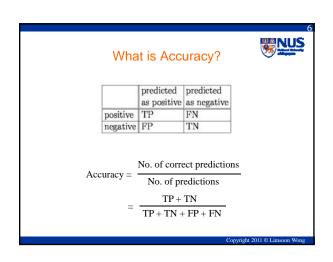
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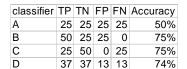








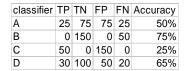
Examples (Balanced Population)



- · Clearly, B, C, D are all better than A
- Is B better than C, D?
- Is C better than B, D?
- . Is D better than B, C?

Accuracy may not tell the whole story

Examples (Unbalanced Population

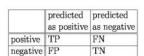


- · Clearly, D is better than A
- Is B better than A, C, D?

Exercise: What is B's Prediction strategy?

High accuracy is meaningless if population is unbalanced

What is Sensitivity (aka Recall)?



No. of correct positive predictions

Sensitivity = wrt positives No. of positives

> ΤP $\overline{TP + FN}$

Sometimes sensitivity wrt negatives is termed specificity

Exercise: Write down the formula for specificity

What is Precision?



	predicted as positive	predicted as negative
positive	TP	FN
negative	FP	TN

No. of correct positive predictions Precision = wrt positives No. of positives predictions

> TP TP + FP

Unbalanced Population Revisited Number



classifier TP TN FP FN Accuracy Sensitivity Precision 25 75 75 25 50% 50% 25% В 0 150 0 50 75% С 50 0 150 0 25% D 30 100 50 20 65% 60% 38%

- . What are the sensitivity and precision of B and C?
- Is B better than A, C, D?

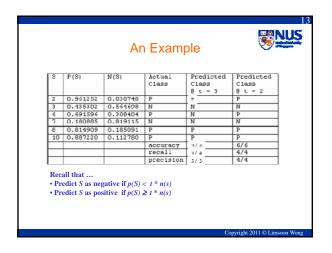
Abstract Model of a Classifier

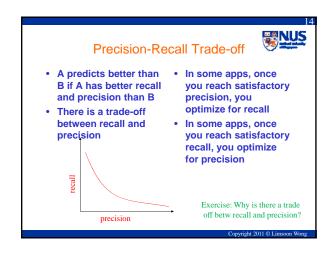


- Given a test sample S
- Compute scores p(S), n(S)
- Predict S as negative if p(S) < t * n(s)
- Predict S as positive if $p(S) \ge t * n(s)$

t is the decision threshold of the classifier

changing t affects the recall and precision, and hence accuracy, of the classifier



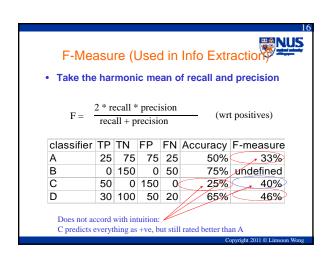


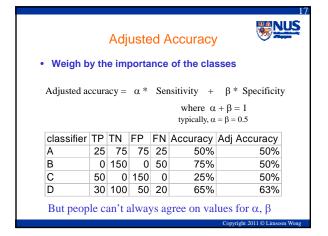
Comparing Prediction Performance · Accuracy is the obvious measure - But it conveys the right intuition only when the positive and negative populations are roughly

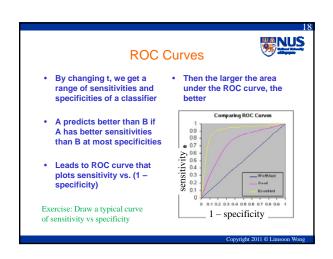
- equal in size
- · Recall and precision together form a better measure - But what do you do when A has better recall than

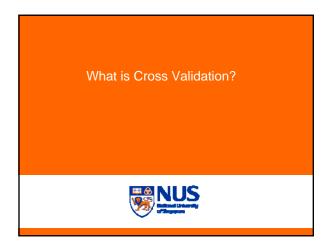
B and B has better precision than A?

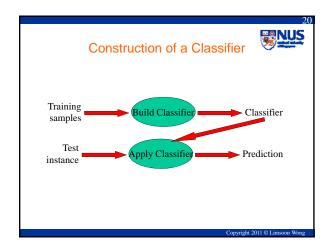
So let us look at some alternate measures

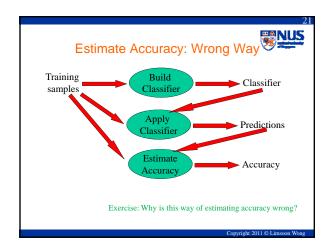


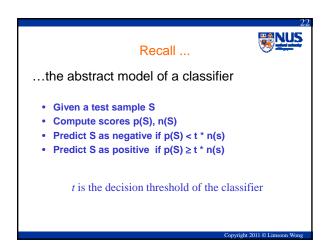




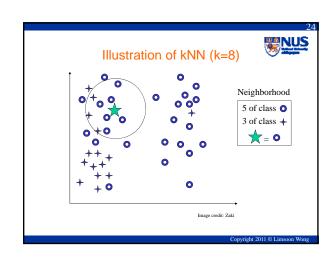


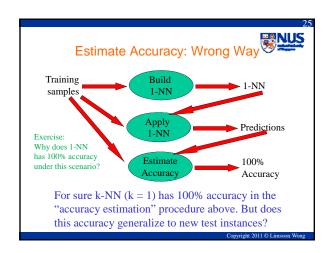


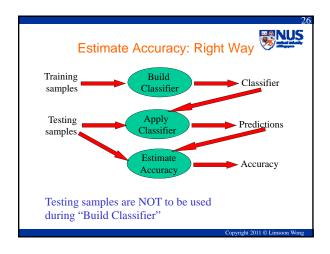




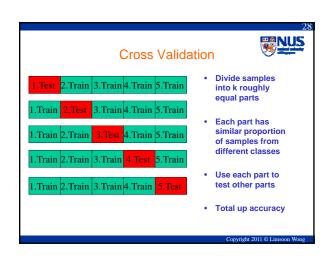
K-Nearest Neighbour Classifier (k-New)
Given a sample S, find the k observations S_i in the known data that are "closest" to it, and average their responses
Assume S is well approximated by its neighbours
p(S) = ∑_{S_i ∈N_i(S) ∩ D^p} n(S) = ∑_{S_i ∈N_i(S) ∩ D^N} where N_i(S) is the neighbourhood of S defined by the k nearest samples to it.
Assume distance between samples is Euclidean distance for now

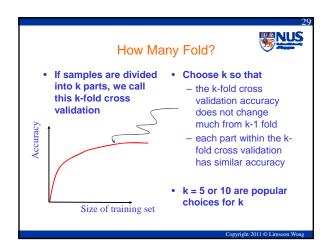


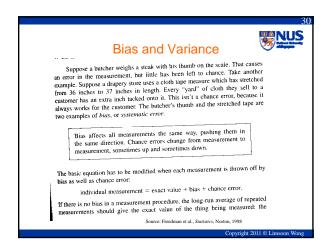


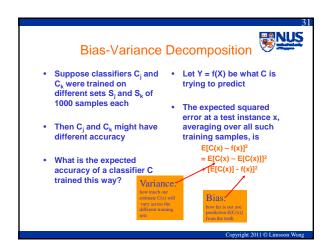


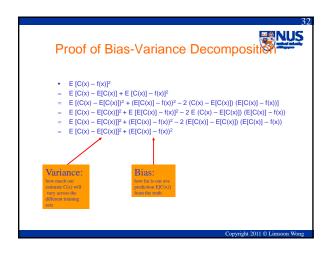
How Many Training and Testing Samples? No fixed ratio between training and testing samples; but typically 2:1 ratio Proportion of instances of different classes in testing samples should be similar to proportion in training samples What if there are insufficient samples to reserve 1/3 for testing? Ans: Cross validation

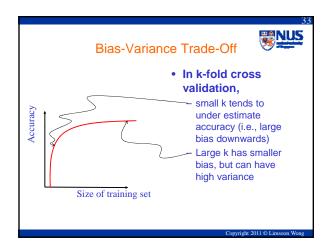


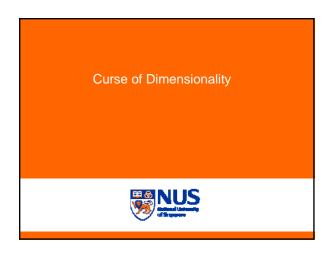


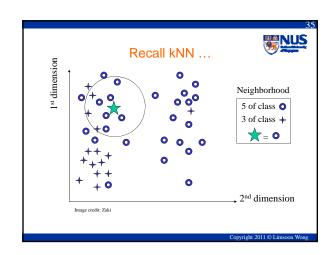


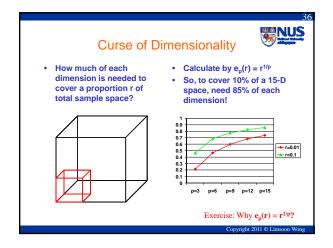












Consequence of the Curse

- Suppose the number of samples given to us in the total sample space is fixed
- · Let the dimension increase
- Then the distance of the k nearest neighbours of any point increases
- · Then the k nearest neighbours are less and less useful for prediction, and can confuse the k-NN classifier

What is Feature Selection?



Tackling the Curse

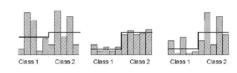


- · Given a sample space of p dimensions
- . It is possible that some dimensions are irrelevant
- Need to find ways to separate those dimensions (aka features) that are relevant (aka signals) from those that are irrelevant (aka noise)

Signal Selection (Basic Idea)



- · Choose a feature w/ low intra-class distance
- · Choose a feature w/ high inter-class distance



Exercise: Name 2 well-known signal selection statistics

Signal Selection (e.g., t-statistics)



The t-state of a signal is defined as

$$t = \frac{|\mu_1 - \mu_2|}{\sqrt{(\sigma_1^2/n_1) + (\sigma_2^2/n_2)}}$$

where σ_i^2 is the variance of that signal in class i, μ_i is the mean of that signal in class i, and n_i is the size of class i.

Self-fulfilling Oracle



- · Construct artificial dataset with 100 samples, each with 100,000 randomly generated features and randomly assigned class labels
- Select 20 features with the best tstatistics (or other methods)
- · Evaluate accuracy by cross validation using the 20 selected features
- The resulting accuracy can be ~90%
- But the true accuracy should be 50%, as the data were derived randomly

What Went Wrong?



- The 20 features were selected from whole dataset
- Information in the held-out testing samples has thus been "leaked" to the training process
- The correct way is to re-select the 20 features at each fold; better still, use a totally new set of samples for testing

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Concluding Remarks



What have we learned?



- Methodology of data mining
 - Feature generation, feature selection, feature integration
- Evaluation of classifiers
 - Accuracy, sensitivity, precision
 - Cross validation
- · Curse of dimensionality
 - Feature selection concept
 - Self-fulfilling oracle

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Any Questions?



Acknowledgements



 The first two slides were shown to me 10+ years ago by Tan Ah Hwee

References



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